The National Strategies Primary

Securing level 2 in mathematics





Securing level 2 in mathematics



First published in 2009 Ref: 00687-2009BKT-EN

Disclaimer

The Department for Children, Schools and Families wishes to make it clear that the Department and its agents accept no responsibility for the actual content of any materials suggested as information sources in this publication, whether these are in the form of printed publications or on a website.

In these materials, icons, logos, software products and websites are used for contextual and practical reasons. Their use should not be interpreted as an endorsement of particular companies or their products.

The websites referred to in these materials existed at the time of going to print.

Please check all website references carefully to see if they have changed and substitute other references where appropriate.

1

Securing level 2 in mathematics

These materials are intended to support you in ensuring that as many children as possible reach level 2 by the end of Key Stage 1. The guidance identifies key areas of learning that children need to secure to attain level 2 in mathematics. While you will integrate the ideas from these materials into your ongoing planning, you could also use them to plan targeted support for particular groups of children. There is a double-page spread for each of the six areas of mathematics:

- Counting, comparing and ordering numbers
- Understanding addition and subtraction and their relationship
- Using mental calculation strategies to solve problems involving addition and subtraction
- Recognising and describing shapes
- Understanding and using standard units and equipment to measure
- Organising and interpreting data to answer questions

Remember

Every day is a mental mathematics day – ensure that children engage in sustained mental work each day (for at least 10–15 minutes) to secure and develop knowledge, skills and understanding in mathematics. *Don't expect confidence in working mentally if practice and repetition have not taken place.*

Hands-on learning is important – provide appropriate practical equipment for children to use and manipulate, to help them to explore how and why things work and to learn to visualise, describe and represent what is in front of them. *Don't just talk about weighing scales, use one; using apparatus is better than imagining how it works*.

Seeing mathematics through models and images supports learning – help children to see how mathematics works and can be represented through physical objects, pictures or diagrams such as place-value cards, counting sticks, number lines and representations of fractional parts. *Don't expect children to visualise and 'see' how something works if they have no models and images to draw from*.

Talking mathematics clarifies and refines thinking – give children the vocabulary and language of mathematics; provide activities and time for them to use this language to discuss mathematics. Teach children the precision of language, for example, using: sum, difference, quarter of and quarter to, and how to express their reasoning using language such as if...then..., because, cannot be, never, sometimes, always. *Don't expect children to explain or provide reasons if they have no opportunity to use, develop and refine the language they need to do this.*

Make mathematics interesting – share your interest in mathematics with the children. Give children mathematics that engages them in: estimating, for example, how much liquid they would drink in a week, month, year...; testing, for example, how many numbers on a hundred square contain the digit 5 and how many of these are multiples of 5; answering intriguing questions such as how many books there are in the school library, how many in the whole school. *Don't expect children to be interested in mathematics if you don't share an interest and all their mathematics is routine and dull.*

Learning from mistakes should build up children's confidence – look out for common mistakes and talk to the children about what they might do differently. Encourage children to work with a partner and talk about the methods they used. *Don't just tell children something is wrong; help them to see what went right and to identify when it went wrong.*

Counting, comparing and ordering numbers

Level 2 standards to be achieved:

Count forwards and backwards in equal steps
Recognise and describe patterns in sequences and use these to extend them
Compare and order whole numbers to 100, using the value of each digit
Partition two-digit numbers in different ways, including into tens and ones
Round any two-digit number to the nearest 10
Find half and one quarter of shapes and sets of objects

For children to attain level 2, they need to:

- count in ones and tens forwards or backwards from any one-digit or two-digit number, using their understanding of place value to identify which digits will change and how they change
- estimate the number of objects in a set and group them in twos, fives or tens to count them efficiently
- recognise and continue common sequences such as odd or even numbers
- identify significant digits to compare and order a set of numbers up to 100, for example, 43, 73, 63 and 23, 26, 25
- understand and use the < and > symbols when ordering one-digit and two-digit numbers
- use knowledge of the relative value of numbers to position them onto partially marked number lines
- use the language of fractions (half, quarter, whole, halve, equal amount) to explain how to find one half or one quarter of shapes or amounts

Make sure that:

counting forms a regular part of children's daily oral and mental work

you use models and images to demonstrate place value and the relative value of numbers

children use equipment such as beadstrings, partially marked number lines, place-value cards and base-ten apparatus to secure their understanding of place value

you build in frequent opportunities for children to explain their reasoning, for example, describing patterns in a sequence and how they would use these to predict the next term

children solve practical problems involving estimating, counting, ordering and rounding numbers

children position two-digit numbers onto partially marked number lines to support their decisions when ordering numbers or rounding them to the nearest 10

children see, manipulate and generate examples of halves and quarters, using practical equipment to represent parts of a whole

Partially marked number lines



Counting stick spreadsheet or a counting stick



Hundred square or Number grid ITP



50	3
	/
<mark>5</mark> 3	

Place-value cards

Intervention materials

Assessment checklist

'l can' statements	Assessment examples
l can count forwards and backwards in equal steps and describe any patterns in the sequence	 Here are some numbers in a sequence:, 7, 9, 11, 13 Will the following numbers be in the sequence: 3, 16, 21, 58? Explain how you know. Write the missing numbers in this sequence. 53 48 43 38 23 18 Explain how you identified them.
l can explain how to put a set of two-digit numbers in order	If you write these numbers in order, smallest first, which number comes third? 37, 13, 73, 33, 3 Write the same digit in each box to make the number sentence true: $1 > 6$ Now do the same for this number sentence: $1 < 6$
l can partition numbers to 100	There are 10 pencils in each box and four more pencils. How many pencils are there altogether? Write a number into the box to make the statement true: 10 + 15 = 45 KS1 2003 © QCA
l can round any two-digit number to the nearest 10 and explain how I did it	Paul wants to round 26 to the nearest 10. He is not sure whether the answer is 20 or 30.What would you say to help him decide?Place these numbers on the number line: 53, 66, 58.50606070Explain how this helps you round each number to the nearest 10.
l can find half or one quarter of a shape or a group of objects	Make lines on a circular paper plate to form quarters. Place 12 counters onto the plate so that there are the same number of counters on each quarter. Explain how you did this.

Understanding addition and subtraction and their relationship

Level 2 standards to be achieved:

Understand and use the language of addition and subtraction

Identify practical situations in which addition and subtraction can be used

Record addition and subtraction problems in different ways, including number sentences

Understand that subtraction can represent situations involving *taking away* and those involving finding the *difference*

Know that subtraction is the inverse of addition and vice versa

Give the subtraction fact that corresponds to an addition fact and vice versa

For children to attain level 2, they need to:

- recognise and use the vocabulary and language associated with addition and subtraction, including: add, subtract, plus, minus, count on, count back, less than, more than, fewer than, greater than and difference between
- understand that the = sign represents equality rather than the answer to a calculation and use the term 'equals' rather than 'makes'
- know that subtraction can represent a situation involving taking away and can be worked out by counting back from the larger number or counting on from the smaller
- appreciate that subtraction can represent finding the *difference* between two quantities and be able to find this difference
- use their understanding of the inverse relationship between addition and subtraction to derive and record related addition and subtraction number sentences using the = sign, and to solve problems

Make sure that:

daily oral and mental work involves generating subtraction facts from addition facts and vice versa

children have regular opportunities to explain how they decided whether to use addition or subtraction to solve particular problems

you model the correct use of addition and subtraction vocabulary in a variety of contexts and support children towards using the language to explain their thinking and methods

you model how to represent practical situations, using apparatus, pictorial representation and then using number sentences

children have opportunities to choose when to work out subtraction, using a counting back or a counting on method

children experience situations and problems where they need to use inverse operations, for example, to *undo* an operation or to find a missing number, and see these operations modelled

Number lines

Teaching and learning resources

Objects in two colours



Sliding box cards



Addition and subtraction number sentences spreadsheet



Function blocks ITP





Intervention materials

Overcoming barriers in mathematics – level 1 to 2 Can I write addition and subtraction sentences that use the same three numbers and explain how they are linked?

Assessment checklist

'l can' statements	Assessment examples
l can use mathematical words to explain how I solve addition and subtraction problems	Read this problem then explain how you would work it out: Demi has a 20p coin and a 10p coin. How much more money does she need to buy a comic that costs 50p? Write a number sentence to show your answer. Explain how to find the missing number: $-8 = 25$
l can explain how I know whether to use addition or subtraction to solve a problem	Say whether you would use addition or subtraction to solve each of these problems and explain how you know: Jude is five years older than Mark. Mark is seven years old. How old is Jude? There are some yellow and some orange flowers in a vase. There are 14 flowers altogether. Six are yellow. How many are orange?
I can record how I solve addition and subtraction problems	Use equipment, drawing or jottings to solve this problem: Samir is running a 50-metre potato race. He drops his potato after 18 metres. How much further does he have to go?
l can solve subtraction problems by taking away or by counting on	Explain your method for each of these problems: Jason took 40p to the school fete. He has spent 15p. How much money does he have left? Peter is 12 and Casey is 9. How much older is Peter than Casey?
l can say the subtraction sentence that matches an addition sentence and the other way round	Place the numbers 6, 15 and 9 into these number sentences: + = = ; - = = Find as many addition and subtraction sentences as you can that use these numbers: 26, 18, 8, 10, 16, 34

Using mental calculation strategies to solve problems involving addition and subtraction

Level 2 standards to be achieved:

Add or subtract a one-digit number to or from a one-digit or two-digit number

Add or subtract a multiple of 10 to or from a two-digit number

Understand how to work out subtraction by both counting back and finding the difference

Choose appropriate operations and resources to solve problems involving addition and subtraction

Select an appropriate method by considering the numbers involved and explain this method, using the language of addition and subtraction

Record how problems were solved, using pictorial representations, number lines and number sentences

For children to attain level 2, they need to:

- add several numbers, using the fact that the order can be changed, for example, finding three numbers that total 20 or finding 13 + 6 + 7 by using 13 + 7 + 6 = 20 + 6
- begin to use known addition and subtraction facts to calculate efficiently
- bridge through a multiple of ten when adding or subtracting over tens boundaries
- use known facts and place value to add or subtract multiples of 10
- partition two-digit numbers when it makes calculation more efficient
- understand that subtraction can be worked out by counting up from the smaller to the larger number to find the difference and that this can be an efficient method when the numbers are close together
- read, interpret and write number sentences, using appropriate words and symbols

Make sure that:

children rehearse and use addition and subtraction facts regularly in daily oral and mental work

children use partially marked number lines and then begin to draw their own number lines to record addition and subtraction methods

you plan frequent opportunities for children to explain their methods and to discuss and compare alternative methods

you model different ways of recording mental methods and encourage children to use pictures and jottings to help them carry out mental calculations

children regularly receive opportunities to use addition and subtraction to solve practical and word problems, including those involving money and measures

you discuss with children how the numbers involved in a calculation might lead to a particular method and why it is appropriate

Counting on and back ITP or a beadstring



Number lines



Assessment checklist

Hundred square

1	2	3	4	5	6	7	8	9	10	
11	12	13	14	15	16	17	18	19	20	75 45
21	22	23	24	25	26	27	28	29	30	56, 66
31	32	33	34	35	36	37	38	39	40	
41	42	43	44	45	46	47	48	49	50	
51	52	53	54	55	56	57	58	59	60	6 + 10 = 16
61	62	63	64	65	66	67	68	69	70	16 + 10 = 26
71	72	73	74	75	76	77	78	79	80	26 + 10 = 36 36 + 10 = 46
81	82	83	84	85	86	87	88	89	90	
91	92	93	94	95	96	97	98	99	100	36 + 20 = 56

Intervention materials

Overcoming barriers in mathematics – level 1 to 2
Can I say what needs to be added to a two-digit number to make the next multiple of ten?
Can I add and subtract multiples of ten?
Can I add or subtract a one-digit number to or from a two-digit number (bridging through a multiple of ten)?
Can I find the difference between a pair of numbers?
Can I work out and record the information I need to use to solve a puzzle or problem?

'l can' statements	Assessment examples
l can add or subtract a one-digit number to or from a two-digit number	Connor drew this number line. What calculation did he work out? 35 40 42 Draw your own number line to show how you would work out 37 + 8.
l can add or subtract a	What number is 30 less than 64? Explain your method.
multiple of 10 to or from a	What is the missing number in the number sentence below? How do you know?
two-digit number	57 + = 97
l can subtract by counting	Work out these two calculations: 32 – 5 and 32 – 29
back or by finding the	Explain how you did each subtraction. Did you choose the same method?
difference	If not, why not?
l can choose how to solve	Megan and Jack are growing beans. Megan's plant is 25cm tall. Jack's is 38cm tall.
a problem and explain my	How much taller is Jack's plant than Megan's? Explain how you worked this out.
method	Jess has saved 62p. She spends 5p. How much money does she have left?
l can record my working	Work out the difference between the number of boys in your class and the
for an addition or	number of girls. Record how you solved the problem so that someone else could
subtraction problem	understand what you did.

Recognising and describing shapes

Level 2 standards to be achieved:

Recognise and name common 2-D and 3-D shapes in different orientations
Describe properties of common 2-D and 3-D shapes, using mathematical terms
Make and talk about shapes, referring to their features or properties
Sort 2-D or 3-D shapes according to one or more criteria
Visualise familiar 2-D and 3-D shapes
Solve simple problems involving 2-D and 3-D shapes

For children to attain level 2, they need to:

- identify and describe 2-D shapes, including squares, triangles, circles, pentagons and hexagons, using properties such as number of sides and corners
- handle common 3-D shapes and explore their properties, such as the number and shape of faces and the number of corners
- consider what is the same and what is different about two or more shapes
- sort shapes, using one criterion initially, and place them in tables and sorting diagrams
- recognise that a shape does not change when it is in a different orientation
- recognise what changes and what stays the same when shapes are moved or enlarged

Make sure that:

shape and space activities are included in oral and mental work and include opportunities for discussion and reasoning

children have opportunities to create 2-D shapes, including use of squared and isometric paper

children have opportunities to create 3-D models, using construction kits, and to explore and discuss their properties

children experience practical hands-on activities involving shapes rather than simply responding to representations of them

you build on children's experience of creating, drawing and manipulating shapes, helping them to visualise familiar shapes by hiding and revealing the shapes

you model the use of mathematical language, display shape vocabulary and encourage children to use it accurately

children are given opportunities to recognise and talk about shapes in a variety of contexts, including photographs, pictures, puzzles and the indoor and outdoor environment

children discuss the properties of the same shape when it is placed in different orientations or enlarged



Artstraws or construction kits



Assessment checklist



Polygon ITP



Guess my number or shape spreadsheet

And Searche Spin teacher Select	
Bar No Low	
can be	The plane has a set of the set of
	tan te

Intervention materials

Overcoming barriers in mathematics – level 1 to 2 Can I name and describe 2-D and 3-D shapes? Can I find similarities and differences between shapes and use these to sort

between shapes and use these to sort into sets I can label?

'l can' statements	Assessment examples
I can recognise and	Identify the shapes that are pentagons. Explain how you know.
and 3-D shapes	
l can describe shapes, using mathematical words	Pick up and look carefully at these three shapes. Do they all have straight edges and flat faces? What else is the same about them? What is different?
	Look at this picture. Don't let your partner see it. Using the names of shapes, tell your partner how to draw it.
l can sort shapes and explain how I sorted them	Rick sorts these shapes into those with five flat faces and those with four or fewer flat faces. Decide which shapes will go in each set. Now choose your own way to sort this set of shapes. Explain how you have done it.
I can draw shapes of different sizes and decide if they are the same or not.	What is the same and different about these three shapes? What mathematical language can you use to describe them?
l can visualise shapes	Imagine a cube. Four faces are yellow, the rest are blue. How many faces are blue? Imagine a pyramid with a square face. What shapes are the other faces? How many vertices does it have? How many edges?

Understanding and using standard units and equipment to measure

Level 2 standards to be achieved:

Use uniform non-standard and standard units to measure
Choose appropriate equipment to measure length, mass and capacity
Read scales to the nearest labelled division
Use experience of measurement to make sensible estimates and discuss them, using the language of measures

Solve practical problems using measures

Use a time line marked in quarter-hour intervals to order events

For children to attain level 2, they need to:

- measure, using a wide range of measuring instruments
- use measurement to solve practical problems
- understand the limitations of using non-standard units of measure and the benefits of using standard units
- recognise common standard units of measurement for length, mass and capacity
- begin to get a feel for benchmark measurements, such as how heavy 1kg of sugar feels or which containers hold about 1 litre
- read the numbered divisions on a scale and interpret the divisions in between
- know and use the relationship between units of time
- read the time to the nearest quarter hour and interpret a time line

Make sure that:

measurement activities are included in oral and mental work

you provide opportunities to discuss the units used to measure length, mass, capacity and time

children have opportunities to discuss and compare measures, using uniform non-standard units, enabling them to recognise the need for having standard units of measure

children have opportunities to make their own scales, using uniform measures

children understand how they can use their number line skills to help them read scales

you draw on cross-curricular opportunities to offer children practical opportunities to apply their measurement skills in context

children hear and use the language of measures when measuring, estimating, comparing and sorting



Counting stick or counting stick with further options spreadsheet

g 0	100	200	300	400	500	600	700	800	900	1000
kg										
-										

Tell Time and Ruler ITPs



Clocks and timelines



A wide selection of measuring instruments



Intervention materials

Overcoming barriers in mathematics – level 1 to 2

Can I read a scale to find out how long or heavy something is?

Can I choose suitable units to measure?

'l can' statements	Assessment examples				
l can choose a suitable unit of measure	Suggest sensible units you might use to measure: the height of your table; how much water is in a cup; the weight of your reading book; how long it takes you to wash your hands.				
l can choose a sensible measuring instrument	Choose a piece of equipment to help you measure: the weight of your shoe; how long the classroom is; how long this lesson lasts; how much water a cup holds.				
l can read a scale to take a measurement	How long is this line? Now draw a line 2cm longer than this one.				
l can make a sensible estimate for a measurement	Find an object in the classroom that you think is about 10cm long. About how heavy do you think your pencil case is?				
l can solve problems by measuring	If I program my floor robot to go forward 3 metres, is there enough room? How could you measure to find out?				
l can use clocks and time lines to tell the time and order events	What time does this clock show? Draw a clock showing the time half an hour later. Show your school day on this time line. When do you leave home, have breaks, go back home, etc?				
	++++ ++++ ++++ ++++ ++++ ++++ ++++ ++++ ++++ ++++ ++++ ++++ +++++ +++++ +++++ +++++ +++++ ++++++ +++++++ ++++++++ ++++++++ +++++++++ +++++++++++ ++++++++++++++++ ++++++++++++++++++++++++++++++++++++				

Assessment checklist

Organising and interpreting data to answer questions

Level 2 standards to be achieved:

Sort objects using more than one criterion

Organise data into lists and tables

Represent data, using pictograms or block graphs where one symbol represents one unit, including through the use of ICT

Begin to read data from pictograms where each symbol represents more than one unit and from bar graphs where the scale is in 2s, 5s or 10s

Answer questions by interpreting data from lists, tables, pictograms, block or bar graphs

Collect, sort and represent data to answer questions and pose and respond to new questions

For children to attain level 2, they need to:

- decide where to place objects on sorting diagrams such as Venn and Carroll diagrams, including those involving two criteria, and explain decisions
- recognise the importance of including titles and labels when organising data into lists and tables and the need for a key when creating pictograms
- interpret and read data presented as pictograms, block and bar graphs
- realise that pictograms, block and bar graphs can be organised so that information runs vertically or horizontally and be able to interpret both orientations
- read titles and labels of lists, tables or graphs carefully in order to identify the information required to answer a question

Make sure that:

children have experience of sorting objects physically, for example, into hoops, before being asked to sort them onto diagrams such as Venn or Carroll diagrams, and choose their own criteria to classify objects

you show children how Venn and Carroll diagrams involving one criterion can be adapted to incorporate a second criterion

children have practical experience of creating pictograms and block graphs, through using counters or physical blocks, before moving into drawing graphs

you help children to understand the need for non-unit scales on graphs, for example, scales marked in 2s, 5s and 10s

children solve problems involving comparing or combining more than one piece of data, for example, how many more boys than girls are there in the class, how many children altogether?

children are given opportunities to work through the whole data-handling cycle, including suggesting a line of enquiry and discussing what data to collect and how

you draw on opportunities from other curricular areas and real-life opportunities to give children meaningful experiences of handling data

Carroll diagram spreadsheet



Data handling ITP



Assessment checklist

Physical graphs, for example using blocks



Blank sorting diagrams such as Venn diagrams



Intervention materials

Overcoming barriers in mathematics – level 1 to 2

Can I use a table, pictogram or block graph to answer questions?

Can I organise a set of objects or information, using properties that they do or do not have in common?

'l can' statements	Assessment examples				
<i>I can sort objects and explain how I sorted them</i>	Choose your own headings to sort a set of 0 to 9 cards. Explain how you sorted them. Look at this Carroll diagram. Where should 15 go?				
l can organise information into lists and tables	Write the numbers from 1 to 30 into a table to show which are multiples of 5. What do you notice?				
l can create a pictogram or block graph to show information	Find out how many girls and how many boys are in your class. Show this information in a table and in a pictogram.				
I can read information from	Ages of children in our classes Cla	Class 2 made a graph.			
tables and graphs and use this to answer questions	Be a How year	How many children are five years old?			
	Wh 2	What is the total number of children in the class?			
	0 5 years 6 years 7 years KS1 : age	KS1 2003 © QCA			
l can suggest what information to collect and how to do it in order to solve a problem	The school cook wants to find a new meal Talk about how you could help her to choo be popular.	that children would like to eat. ose a meal to cook that would			

Where can I find the resources?

ICT resources

ITPs (Interactive Teaching Programs)



These programs can be downloaded from www.standards. dcsf.gov.uk/nationalstrategies. Navigate to the Primary Mathematics Framework area and then to the Mathematics resource library. Refine the results by filtering down to the Interactive Teaching Programs.

Difference ITP

Spreadsheets

+	14			34	
4		79			
9				43	
	48				
5			68		
Reset	Click on cells to hide and reveal contents				

These programs can be downloaded from www.standards. dcsf.gov.uk/nationalstrategies. Navigate to the Primary Mathematics Framework area and then to the Mathematics resource library, then search for spreadsheets.

Addition and subtraction facts spreadsheet

Intervention materials

Overcoming barriers in mathematics – helping children move from level 1 to level 2

This is a booklet with a set of materials, based on a CD-ROM, designed to help teachers move children from level 1 into level 2. Further information about these materials can be found at www.standards.dcsf. gov.uk/nationalstrategies. Search using reference 00021-2009.

Supporting children with gaps in their mathematical understanding – Wave 3

The Wave 3 mathematics pack aims to help teachers identify and address gaps in learning for children who are working significantly below age-appropriate levels. They can be downloaded from www.standards.dcsf.gov.uk/nationalstrategies. Search using reference 1166-2005.

Acknowledgements

Two questions taken from Key Stage 1 Maths 2003. © Qualifications and Curriculum Authority.

Used with kind permission.

QCA test questions and mark schemes can be found at www.testbase.co.uk

Audience: Headteachers, mathematics subject leaders, teachers, LA consultants Date of issue: 08-2009 Ref: **00687-2009BKT-EN**

Copies of this publication may be available from: **www.teachernet.gov.uk/publications**

You can download this publication and obtain further information at: **www.standards.dcsf.gov.uk**

Copies of this publication may be available from: DCSF Publications PO Box 5050 Sherwood Park Annesley Nottingham NG15 ODJ Tel 0845 60 222 60 Fax 0845 60 333 60 Textphone 0845 60 555 60 email: dcsf@prolog.uk.com

© Crown copyright 2009 Published by the Department for Children, Schools and Families

Extracts from this document may be reproduced for non-commercial research, education or training purposes on the condition that the source is acknowledged as Crown copyright, the publication title is specified, it is reproduced accurately and not used in a misleading context.

The permission to reproduce Crown copyright protected material does not extend to any material in this publication which is identified as being the copyright of a third party.

For any other use please contact licensing@opsi.gov.uk www.opsi.gov.uk/click-use/index.htm





department for children, schools and families